Final Element of Periodic Table is Element N 137

AV Morozkin* and R Nirmala

1Department of Chemistry, Moscow Lomonosov State University, Russia
2Department of Physics, Indian Institute of Technology Madras, India

Abstract
This work reports the model of single-electron ion with average ionisation potential accuracy of 0.00116%. This model confirms the thesis about final/last element of Periodic Table with N 137 and it permits to construct the full variant of Periodic Table.

Keywords
Single-electron ion, Ionization potential, Periodic table

Introduction

The well-known Bohr model of the atom [1] is basic model for explanation of electronic shell structure. Bohr model shows that the final/last element of the Periodic Table is N 137 from the condition $v_e < c$ (here $v_e$ the speed of electron and $c$ the light speed). However the ionization potentials of the singe-electron atom/ions from H to Kr$^{39+}$ [2-6] show systematic deviation from Bohr model of atom (Figure 1). This deviation reaches value of 1.6885% for Kr$^{35+}$ with average accuracy of $\pm$ 0.5764% and minimal deviation of 0.020% for Li$^{2+}$ ion (Table 1).

The planetary model of atom based on well-known Rutherford and Kepler planetary models [1] has better agreement with experiment than Bohr model of atom for the ionization potentials of H, D and T (inset in Figure 1), but this model shows deviation from the experimental data in case of single-electron ions with Z bigger than 1.

The models with such deviations from experimental data does not permit to do conclusion concerning final element of the Periodic Table and the problems for final element of Periodic Table and full variant of the Periodic Table remains unclear.

The relativistic models of the single-electron ion (atom) (Table 1) based on well-known Einstein special relativity [1] permits to improve the Bohr atom and planetary models. These relativistic models improve the accordance of calculated and experimental data for Z bigger than 1 (Table 1 and Figure 1).

However, the resulting deviation of the experimental data obtained from planetary-relativistic model shows presence the additional component in the interaction of ‘electron-atomic nucleus’ (Figure 2). This empirical component proportional to the $\sim Z^{10/3}$ may be due to e.g. some asymmetry of...
Moreover, the deviations of this model from experiment are close to the experimental estimated standard deviation (ESD). Formally, the electron full energy and atomic nucleus full energy in this model may be calculated (Figure 3).

Anyway, the final planetary-relativistic model with this empirical component (Table 1) has the best agreement with experimental data (Figure 1).

Figure 1: Accordance of the different models of single-electron ions with experimental data: The $E/I_{\text{experim}}$ ratio vs element number $Z$. Inset in Figure: The $E/I_{\text{experim}}$ ratio for hydrogen (H), deuterium (D) and tritium (T). ($E$ the calculated energy of ‘electron-atomic nucleus' bond in the different models of single-electron ions and $I_{\text{experim}}$ the experimental ionization potential [2-6]).

Figure 2: Deviation of planetary-relativistic model from the experimental data: $\Delta E/E_0$ ratio vs. element number $Z$ (here $\Delta E = E - I_{\text{experim}}$, $E_0 = m_e e^4/\left(8\epsilon_0^2\hbar^2\right)$). Inset in Figure: $\Delta E/E_0$ vs $Z^{10/3}$.
The details of the Bohr model of atom, planetary, relativistic, planetary relativistic and final planetary-relativistic models are summarized in Table 1. The resulting expression of final planetary-relativistic model is:

\[ E = m_0 c^2 \left[ \frac{(1 - v^2/c^2)^{1/2} - 1}{m_0 + M} \right], \]

where \( v = (Z + A Z^{7/3}) e^2 / (2 \varepsilon_0 h n) \) and \( A = -2.81 \times 10^{-6} \) (deviation for H\(^+\) is 0.000181%, for Ar\(^{35+}\) is 0.000189%, maximum deviation of 0.00364% for Li\(^{2+}\) and average deviation of 0.00116% is obtained).

Final model gives the full energy of 'electron-atomic nucleus' system with good accuracy. The calculated \( v \) and \( v_e \) speeds (electron speed \( v_e \) and sum of electron and atomic nucleus speeds \( v \)) reach values of \( v = v_e = 0.997753204 \cdot c \) at \( Z = 137 \) and they should be bigger than \( c \) speed at \( Z = 138 \). Even if atomic nucleus with \( Z > 137 \) will stable, the every free electron should fall down on atomic nucleus with well-known reaction of \( \text{p} + e \rightarrow \text{n} + \nu \) \([1]\) that shifts the element number to equal of 137 or less.

So, the \( v_e (v) \) less than \( c \) is condition of the stable electronic shell and the final possible element of Periodic Table with stable atomic nucleus is N 137.

The full variant of the Periodic Table may be constructed using this condition and well-known rules of filling of the electronic shell \([1]\) (Table 2).

The g-elements from 121 to 137 are essentially new elements with orbital quantum number \( l = 4 \). Perhaps, they will demonstrate the magnetic properties, like 3d and 4f elements \([6]\) and they may be interesting for science and technology. Meanwhile, the final 137 element will has the full electronic shell \( 1s^2 2s^2 2p^6 3s^2 3p^6 4s^2 3d^{10} 4p^6 5s^2 4d^{10} 5p^6 6s^2 4f^{14} 5d^{10} 6p^6 7s^2 5f^{14} 6d^{10} 7p^6 8s^2 5g^{17} \).

On one hand these are evident results and electron speed close to light speed is evident factor of heavy element synthesis, on the other hand this full variant of Periodic Table permit to estimate the perspectives of new elements for materials and technology. E.g. from empirical rule the stable element N 106 should have the melting temperature about 4380 K (for comparison: The Cr, Mo and W elements from this group have the melting temperature of 2130, 2890 and 3680 K \([6]\), respectively).

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References

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